

For all problems solve over the complex numbers ($a + bi$). Simplify all answers when possible for full credit.

WORK is required and graded. List your answers separately as two distinct answers.

1. Solve by factoring: $x^2 - 9x - 36 = 0$

$$(x+3)(x-12) = 0$$

$$\begin{aligned} x+3 &= 0 & x &= 12 \\ x &= -3 \end{aligned}$$

1. $x = \underline{-3}$

$x = \underline{12}$

2. Solve by using square roots: $100x^2 - 56 = 0$

$$100x^2 = 56$$

$$x^2 = \frac{56}{100}$$

$$x = \pm \frac{\sqrt{56}}{10} = \pm \frac{2\sqrt{14}}{10} = \pm \frac{\sqrt{14}}{5}$$

$$\begin{array}{c} 56 \\ \sqrt{ } \\ \begin{array}{c} 4 \\ \diagdown \\ 2 \quad 2 \end{array} \quad \begin{array}{c} 14 \\ \diagup \\ 2 \quad 7 \end{array} \end{array}$$

2. $x = \underline{\frac{\sqrt{14}}{5}}$

$x = \underline{-\frac{\sqrt{14}}{5}}$

3. Solve using any method: $x^2 + 18x + 81 = 16$

ALT METHOD: $x^2 + 18x + 81 = 16$ $\begin{array}{c} -16 \\ -16 \end{array}$

$$(x+9)(x+9) = 16 \quad x^2 + 18x + 65 = 0$$

$$(x+9)^2 = 16 \quad (x+5)(x+13) = 0$$

$$x+9 = \pm 4 \quad x = -5 \quad x = -13$$

$$x = -9 \pm 4 \rightarrow -5 \quad -13$$

4. Solve using any method: $6x^2 - 13x - 8 = 0$

$$\left(\frac{6x+3}{3}\right)\left(\frac{6x-16}{2}\right) = 0 \quad \begin{array}{c} 3=-48 \\ | \\ 3+16=-13 \end{array}$$

$$(2x+1)(3x-8) = 0$$

$$\begin{array}{l} 2x+1=0 \quad 3x=8 \\ 2x=-1 \quad x=\frac{8}{3} \\ x=-\frac{1}{2} \end{array}$$

3. $x = \underline{-5}$

$x = \underline{-13}$

$\underline{-\frac{1}{2}}$

$x = \underline{\frac{8}{3}}$

5. Solve using any method: $100x^2 + 9 = 0$

$$\begin{array}{r} -9 \quad | \quad -9 \\ \hline 100x^2 = -9 \\ \hline 100 \end{array}$$

$$\sqrt{x^2} = \sqrt{-\frac{9}{100}} \rightarrow$$

5. $x = \underline{-\frac{3i}{10}}$

$x = \underline{\frac{3i}{10}}$

$x = \underline{\pm \frac{\sqrt{-9}}{\sqrt{100}}} = \underline{\pm \frac{-3i}{10}}$

$$a=6 \quad b=2 \quad c=5$$

6. Solve using the quadratic Formula: $6x^2 + 2x + 5 = 0$

$$\Delta = b^2 - 4ac$$

$$= (2)^2 - 4(6)(5)$$

$$= 4 - 120$$

$$= -116$$

$\begin{array}{c} 116 \\ \diagdown \quad \diagup \\ 2 \quad 58 \\ \textcircled{2} \quad \textcircled{2} \quad 29 \end{array}$

$$x = \frac{-b \pm \sqrt{\Delta}}{2a}$$

$$= \frac{-2 \pm \sqrt{-116}}{2(6)}$$

$$= \frac{-2 \pm i\sqrt{116}}{12} = \frac{-2 \pm 2i\sqrt{29}}{12} = \frac{-2 \pm 2i\sqrt{29}}{12}$$

$$x = \frac{-1}{6} + \frac{i\sqrt{29}}{6}$$

$$x = \frac{-1}{6} - \frac{i\sqrt{29}}{6}$$

$$= \frac{-1}{6} - \frac{i\sqrt{29}}{6}$$

$$= \frac{-2}{12} \pm \frac{2i\sqrt{29}}{12}$$

7. If $A = 8 - 6i$ and $B = 10 - 20i$ find the following:

$$7. A + B = 18 - 26i$$

a. $A + B$

$$8 - 6i + 10 - 20i$$

$$18 - 26i$$

b. $(A)(B)$

$$(8 - 6i)(10 - 20i)$$

$$= 80 - 160i - 60i + 120i^2 \leftarrow i^2 = -1$$

$$= 80 - 220i - 120$$

$$= -40 - 220i$$

$$(A)(B) = -40 - 220i$$

$$120 \cdot i^2 = -120$$

8. Write the quadratic equation in its factored form: $4x^2 - 8x - 21$

$$\left(\frac{4x+6}{2}\right) \left(\frac{4x-14}{2}\right)$$

$$(2x+3)(2x-7)$$

$$8. (2x+3)(2x-7)$$

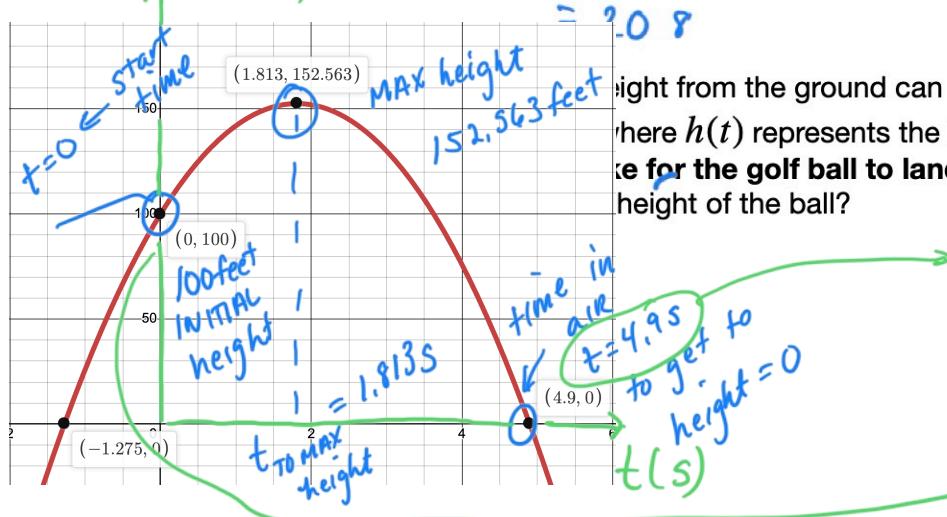
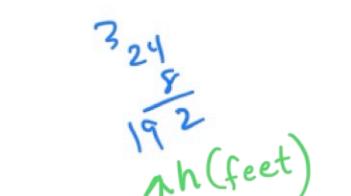
$$\begin{array}{r} \cancel{a} \cancel{c} = -84 \\ 6 \cancel{-} 14 = -8 \end{array}$$

9. Determine the DISCRIMINANT and state the type (imaginary or real) and number of solutions the quadratic equation: $6x^2 + 4x - 8 = 0$

$$9. \text{ Discriminant } (\Delta) = 208$$

Type and number of solutions:

2 Real Sol.



Height from the ground can be modeled by the function $h(t) = -16t^2 + 100$. At what time t will the ball hit the ground? (Round to the nearest tenth)

$$10. t = 4.9 \text{ seconds}$$

$$\text{Initial height} = 100 \text{ ft}$$

